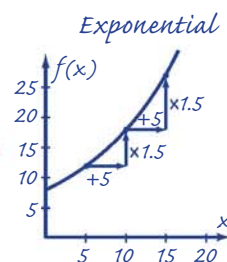


- c. Exponential functions have the add-multiply property. Notice that adding 5 to x results in multiplying the corresponding $f(x)$ -value by 1.5. Make a table of values ending at $x = 20$. The answer is $f(20) = 40.5$.

	x	$f(x)$	
	5	12	
+5 (10	18) $\times 1.5$
+5 (15	27) $\times 1.5$
+5 (20	40.5) $\times 1.5$



EXAMPLE 3 Describe the effect on y of doubling x if

- y varies directly with x .
- y varies inversely with the square of x .
- y varies directly with the cube of x .

SOLUTION

- y is doubled (that is, multiplied by 2^1).
- y is multiplied by $\frac{1}{4}$ (that is, multiplied by 2^{-2}).
- y is multiplied by 8 (that is, multiplied by 2^3).

EXAMPLE 4 Suppose that f is a direct-square power function and that $f(5) = 1000$. Find $f(20)$.

SOLUTION

Because f is a power function, it has the multiply-multiply property. Express $x = 20$ as $x = 4 \cdot 5$. Multiplying x by 4 will multiply the corresponding $f(x)$ -value by 4^2 because f is a direct square, so

$$f(20) = f(4 \cdot 5) = 4^2 \cdot f(5) = 16 \cdot 1000 = 16,000$$

EXAMPLE 5 *Radioactive Tracer Problem:* The compound 18-fluorodeoxyglucose (18-FDG) is composed of radioactive fluorine (18-F) and a sugar (deoxyglucose). It is used to trace glucose metabolism in the heart. 18-F has a half-life of about 2 h, which means that at the end of each 2-hour time period, only half of the 18-F that was there at the beginning of the time period remains. Suppose a dose of 18-FDG was injected into a patient. Let $f(x)$ be the number of *microcuries* (μCi) of 18-FDG that remains over time x , in hours, as shown in the table.

$x(\text{h})$	$f(x)$ (μCi)
2	5
4	2.5
6	1.25
8	0.652

- Find the number of microcuries that remains after 12 h.
- Identify the pattern these data points follow. What type of function shows this pattern?
- Why can't you use the pattern to find $f(25)$?

